

Adding & Subtracting Radicals

Notes: Lesson 3

When adding/subtracting radical expressions, the type of radical AND what's underneath it must be exactly the same.

Example 1... If possible, add or subtract each radical expression.

a. $2\sqrt{7} + 3\sqrt{7}$

$$5\sqrt{7}$$

b. $7\sqrt[4]{x} - 2\sqrt[3]{x}$

not possible to subtract

c. $14\sqrt[3]{2} + 3\sqrt[3]{4}$

not possible to add

d. $4\sqrt{xy} + 5\sqrt{xy}$

$$9\sqrt{xy}$$

Example 2... Simplify each radical, then add/subtract if possible.

a. $3\sqrt{20} - \sqrt{45} + 4\sqrt{80}$
 $\sqrt{4^2 \cdot 5} \quad \sqrt{9 \cdot 5} \quad \sqrt{16^2 \cdot 5}$

$$3 \cdot 2\sqrt{5} - 3\sqrt{5} + 4 \cdot 4\sqrt{5}$$

$$6\sqrt{5} - 3\sqrt{5} + 16\sqrt{5}$$

$$\boxed{19\sqrt{5}}$$

b. $3\sqrt[3]{16} - 4\sqrt[3]{54} + \sqrt[3]{128}$
 $\sqrt[3]{8^2 \cdot 2} \quad \sqrt[3]{27^2 \cdot 2} \quad \sqrt[3]{64^2 \cdot 2}$

$$3 \cdot 2\sqrt[3]{2} - 4 \cdot 3\sqrt[3]{2} + 4\sqrt[3]{2}$$

$$6\sqrt[3]{2} - 12\sqrt[3]{2} + 4\sqrt[3]{2}$$

$$\boxed{-2\sqrt[3]{2}}$$

c. $\sqrt{50} + 2\sqrt{72} - \sqrt{12}$
 $25^2 \quad 36^2 \quad 4^3$

$$5\sqrt{2} + 2 \cdot 6\sqrt{2} - 2\sqrt{3}$$

$$5\sqrt{2} + 12\sqrt{2} - 2\sqrt{3}$$

$$\boxed{17\sqrt{2} - 2\sqrt{3}}$$

d. $\sqrt[3]{135} - \sqrt[3]{48}$
 $27^5 \quad 8^6$

$$\boxed{3\sqrt[3]{5} - 2\sqrt[3]{6}}$$

Example 3... Use the distributive property to multiply the following binomial expressions.

a. $(2 + 4\sqrt{3})(1 - 5\sqrt{3})$

$$\begin{aligned} & 2 - 10\sqrt{3} + 4\sqrt{3} - 20\sqrt{9} \\ & \quad - 20(3) \\ & \quad - 60 \end{aligned}$$

$$\boxed{-58 - 6\sqrt{3}}$$

b. $(3 + \sqrt{7})(3 - \sqrt{7})$

← conjugates

$$\begin{aligned} & 9 - 3\sqrt{7} + 3\sqrt{7} - \sqrt{49} \\ & \quad - 7 \end{aligned}$$

$$\boxed{2}$$

Remember...